DEVI AHILYA VISHWAVIDYALAYA, INDORE

School of Mathematics

1.1.1
Syllabus of all programs

School of Mathematics, DAVV, Indore

Taking into consideration the recent advances in different areas of mathematics, the board of studies in Mathematics, after discussions with experts, has revised the syllabus of M.Sc./M. A. Mathematics course.

Aims:

1. Strengthening the logical reasoning which is the main ingredient to understand mathematical concepts.
2. Create more interest in the subject and motivate students for self learning.
3. Developing the mathematical skills among the students and preparing them to take up a career in research.

Objectives:

1. To make students understand the techniques of proof in Mathematics and apply suitable techniques to tackle problems.
2. To inculcate the habit of making observations and experimentation and arrive at the final result.
3. Make student acquire the communication skill to present technical Mathematics so as to take up a career in Teaching Mathematics at various levels including schools, colleges, universities, etc.

General e-references:

1. National Programme on Technology Enhanced Learning.(Mathematics)
   http://www.nptelvideos.com/mathematics/
2. Mathematics Video Lectures
   http://freevideolectures.com/Subject/Mathematics
3. MIT Open Course Ware
   http://ocw.mit.edu/courses/audio-video-courses/

e-references pertinent to each course are given at the end of the syllabus of the course.

SCHEME OF EXAMINATION
M.A. /M.Sc. Mathematics.

Semester I

CODE	SUBJECT	L	T	S	C
M 111	Field theory	4	--	2	6
M 112	Real Analysis-I	4	--	2	6
M 113	Topology-I	4	--	2	6
M 114	Complex Analysis-I	4	--	2	6
M 101	Differential Equations-I	4	--	2	6
	Viva-Voce				4

Contact hours	:	30 per week
Valid credits	:	30
L	:	Lecture
S	:	Self Study
T	:	Tutorial
C	:	Credits

* The following notation comprising of three digits is used while numbering the courses.

1. The first digit refers to the semester number i.e. 1,2,3, and 4.
2. The second digit 1 refers to a compulsory course and the second digit 0 refers to an optional course.
3. The third digit refers to the serial number of the course.

SCHEME OF EXAMINATION

M.A. /M.Sc. Mathematics

Semester II

CODE	SUBJECT	L	T	S	C
M 211	Advanced Abstract Algebra	4	--	2	6
M 212	Real Analysis-II	4	--	2	6
M 213	Topology-II	4	--	2	6
M 214	Complex Analysis-II	4	--	2	6
M 201	Differential Equations-II	4	--	2	6
	Viva-Voce				4

Contact hours	:	30 per week
Valid credits	:	30
L	:	Lecture
S	:	Self Study
T	:	Tutorial
C	:	Credits

* The following notation comprising of three digits is used while numbering the courses.

1. The first digit refers to the semester number i.e. 1,2,3, and 4.
2. The second digit 1 refers to a compulsory course and the second digit 0 refers to an optional course.
3. The third digit refers to the serial number of the course.

SCHEME OF EXAMINATION

M.A. /M.Sc. Mathematics

Semester III

CODE	SUBJECT	L	T	S	C
M 311	Integration Theory	4	-	2	6
M 312	Functional Analysis	4	-	2	6
M 313	Partial Differential Equations	4	-	2	6
M 301	Theory of Linear Operators-I	4	-	2	6
M 302	Linear Programming-I	4	-	2	6
	Viva-Voce				4

Contact hours	:	30 per week
Valid credits	:	30
L	:	Lecture
S	:	Self Study
T	:	Tutorial
C	:	Credits

* The following notation comprising of three digits is used while numbering the courses.

1. The first digit refers to the semester number i.e. 1,2,3, and 4.
2. The second digit 1 refers to a compulsory course and the second digit 0 refers to an optional course.
3. The third digit refers to the serial number of the course.

SCHEME OF EXAMINATION

M.A. /M.Sc. Mathematics

Semester IV

CODE	SUBJECT	L	T	S	C
M 411	Mechanics	4	-	2	6
M 401	Theory of Linear Operators - II	4	-	2	6
M 402	Linear Programming -II	4	-	2	6
M 403	Homotopy Theory	4	-	2	6
M 404	Topics In Ring Theory	4	-	2	6
	Minor Project	--	--	--	2*
	Viva-Voce				4

Contact hours	:	30 per week
Credits	:	32
L	:	Lecture
S	:	Self Study
T	:	Tutorial
C	:	Credits

* Minor projects will be based on programming and softwares.

* The following notation comprising of three digits is used while numbering the courses.

1. The first digit refers to the semester number i.e. 1,2,3, and 4.
2. The second digit 1 refers to a compulsory course and the second digit 0 refers to an optional course.
3. The third digit refers to the serial number of the course.

ELECTIVE COURSES

Semester I

CODE	SUBJECT
M 101	Differential Equations-I
M 102	Advanced Discrete Mathematics-I
M 103	Differential Geometry of Manifolds-I

Semester II

CODE	SUBJECT
M 201	Differential Equations-II
M 202	Advanced Discrete Mathematics-II
M 203	Differential Geometry of Manifolds-II

Semester III

CODE	SUBJECT
M 301	Theory of Linear Operators-I
M 302	Linear Programming-I
M 303	Pragramming in C – Theory & Practical
M 304	Mathematics of Finance & Insurance-I

Semester IV

CODE	SUBJECT
M 401	Theory of Linear Operators - II
M 402	Linear Programming-II
M 403	Homotopy Theory
M 404	Topics In Ring Theory
M 405	Algebraic Topology
M 406	Analytical Number Theory
M 407	Abstract Harmonic Analysis
M 408	Mathematics of Finance & Insurance-II

* Those electives will be offered for which expertise is available in the department.

SYLLABUS

M.A./M.Sc. MATHEMATICS

SEMESTER I

M 111 Field theory

M 112 Real Analysis-I

M 113 Topology-I

M 114 Complex Analysis-I

M 101 Differential Equations-I

SEMESTER II

M 211 Module Theory

M 212 Real Analysis-II

M 213 Topology-II

M 214 Complex Analysis-II

M 201 Differential Equations-II

SEMESTER III

M 311 Integration Theory

M 312 Functional Analysis

M 313 Partial Differntial Equations

M 301 Theory of Linear Operators-I

M 302 Linear Programming-I

SEMESTER IV

M 411 Mechanics

M 401 Theory of Linear Operators - II

M 402 Linear Programming -II

M 403 Homotopy Theory

M 404 Topics in Ring Theory

Course Plan: Each course has five units and each unit shall be covered in three weeks on average.

SEMESTER - I

M 111
FIELD THEORY

Pre-requisites: Basics on rings and fields.(relevant parts of reference [1])

Unit I:
Finite & Algebraic extensions, Algebraic closure,

Unit II:
splitting fields and normal extensions, separable extensions,

Unit III:
Finite fields, Primitive elements and purely inseparable extensions.

Unit IV:
Galois extensions, examples and applications,

Unit V:
Roots of unity, Linear independence of characters, cyclic extensions, solvable & radical extensions.

Book Recommended:

1. Serge Lang : Algebra

Reference Books:

1. I.N.Herstein, Topics in Algebra, Wiley Eastern Ltd., New Delhi, 1975.
2. M.Artin, Algebra, Prentice - Hall of India, 1991.
3. N.Jacobson, Basic Algebra, vols I&II, W.H.Freeman,1980.
4. S.Kumaresan, Linear Algebra, A Geometric Approach, Prentice - Hall of India, 2000.
5. D.S.Dummit & R.M.Foote, Abstract Algebra, II Ed, John Wiley & Sons, Inc, New York.

E-references:

1. Notes on Galois Theory, Sudhir R. Ghorpade
   Department of Mathematics, Indian Institute of Technology, Bombay 400 076
   http://www.math.iitb.ac.in/~srg/Lecnotes/galois.pdf

2. Galois Theory, Dr P.M.H. Wilson.
   http://www.jchl.co.uk/maths/Galois.pdf

M 112
REAL ANALYSIS-I

Pre-requisites: Chapters 1 to 5 of reference [1]

Unit I:

The Riemann-Stieltjes Integral Definition and existence of the integral, properties of the integral, integration and differentiation, integration of vector-valued functions, rectifiable curves.

Unit II:

Sequences and Series of Functions Rearrangements of terms of a series, Riemann theorem, pointwise and uniform convergence, Cauchy criterion for uniform convergence, Weiestrass M-test, uniform convergence and continuity, uniform convergence and integration.

Unit III:

Uniform convergence and differntiation, equicontinuous families of functions, the Stone-Weierstrass Theorem, uniform convergence and Riemann-Stieltjes integral,

Unit IV:

Abels test for uniform convergence, Dirichlet's test for uniform convergence.
power series, Abel's theorem.

Unit V:

Functions of Several Variables, derivatives in an open subset of R^n, chain rule, partial derivatives, interchange of the order of differentiation, derivatives of higher orders, inverse function theorem, implicit function theorem, Jacobians, differentiation of integrals, Taylor's theorem, extremum problems with constraints, Lagrange's multiplier method.

Books Recommended:

1. Walter Rudin, Principles of Mathematical Analysis(3rd edition), McGraw-Hill international editions, 1976.
2. T.M. Apostol, Mathematical Analysis(2nd edition), Narosa Publishing House, New Delhi, 1989.

Reference Books:

1. Walter Rudin, Real & Complex Analysis, Tata McGraw-Hill Publishing Co. Ltd., New Delhi, 1966.
2. H.L. Royden, Real Analysis(4th edition), Macmillan Publishing Company, 1993.

M 113
TOPOLOGY – I

Unit I: (Pre-requisites)
Relations,Countable and uncountable sets. Infinite sets and the Axiom of choice. Cardinal numbers and their arithmetic. Schroeder-Bernstein theorem. Cantor's theorem and continuum hypothesis. Zorn's lemma. Well-ordering theorem.

Unit II:
Topological spaces. The order topology. Product topology on X x Y. Bases and subbases. Subspaces and relative topology.

Unit III:
Closed sets and limit points. Closure of a set. Dense subsets. Interior, exterior and boundary of a subset.

Unit IV:
Continuous Functions and homeomorphisms. The product topology. The metric topology. The quotient topology

Unit V:
Connected spaces. Connectedness on the real line. Components. Locally connected spaces. Connectedness and product spaces

Books Recommended :
1. James R. Munkres, Topology (Second edition), Prentice-hall of India
2. George F. Simmons, Introduction to topology and modern analysis, McGraw Hill Book Company Inc.

References :
1. N. Bourbaki, General topology, Springer-verlag.
2. K.D.Joshi, Introduction to topology, Wiley Eastern.
3. J.L.Kelley, General topology, Affiliated East-West press Pvt Ltd.

E-references:

1. Topology Course Lecture Notes Aisling McCluskey and Brian McMaster
   http://at.yorku.ca/i/a/a/b/23.htm
2. Notes on Introductory Point-Set Topology, Allen Hatcher
   http://www.math.cornell.edu/~hatcher/Top/TopNotes.pdf
3. Introduction to Topology, Renzo
   http://www.math.colostate.edu/~renzo/teaching/Topology10/Notes.pdf
4. Topology Lecture Notes, Thomas Ward, UEA
   http://www.uea.ac.uk/~h720/teaching/topology/materials/topology.pdf

M 114
COMPLEX ANALYSIS-I

Pre-requisites:
Basic Metric space theory: relevant parts of reference [1]

Unit I: Algebra of complex numbers, geometric aspects like equations to straight lines, circles, analytic functions, exponential ,trigonometric, hyperbolic functions, Branches of many valued functions with special reference to arg z, log z,and complex exponents.

Unit II:
Complex integration, Cauchy 's Theorem , Cauchy's Integral formula, Higher ordered derivatives, Morera's theorem, Liouville's theorem, Fundamental theorem of algebra.

Unit III:
Taylor's theorem, Maximum Modulus Principle, Schwarz Lemma.

Unit IV:
Isolated singularities, Meromorphic functions, Laurent's series, Argument Principle, Rouche's theorem.

Unit V:
Residues, Cauchy's Residue theorem, evaluation of integrals, , their properties and classification, definitions and examples of conformal mappings, Hadamard three circles theorem.

Books Recommended:

1.J.B.Conway : Functions of one Complex variable, Springer-verlag.
2. S.Ponnusamy : Foundations of Complex Analysis, Narosa Pub, `97

References :

1. George F. Simmons, Introduction to topology and modern analysis, McGraw Hill Book Company Inc.
2. Alfohrs : Complex Analysis

E-references:

1. Introduction to Complex Analysis
   http://rutherglen.science.mq.edu.au/wchen/lnicafolder/lnica.html

2. Complex Analysis
   www.umn.edu/~arnold/502.s97/complex.pdf

M 101
DIFFERENTIAL EQUATIONS-I

Pre-requisites: Chapters 1 to 5 of reference [2]

Unit I:
Initial value problems and the equivalent integral equation, mth order equation in d-dimensions as a first order system, concepts of local existence, existence in the large and uniqueness of solutions with examples. Bassic theorems: Ascoli- Arzela theorem, a theorem on convergence of solutions of a family of initial value problems. Picard-Lindel of theorem, Peano's existence theorem and corollary

Unit II:
Maximal interval of existence, Extension theorem and corollaries, Kamke's convergence theorem, Knesser's theorem. (Statement only) Differential inequalities and uniqueness : Gronwall's inequality, Maximal amd minimal solutions, Differential inequalities.

Unit III:
A theorem of Wintner, Uniqueness theorems, Nagumo's and Osgood's criteria.Egres points and Lyapunov functions, Successive approximations.

Unit IV:
Linear differential equations : Linear systems, Variation of constants, reduction to smaller systems, Basic inequalities, constant coefficients.

Unit V:
Floquet theory, adjoint systems, Higher order equations. Dependence on initial conditions and parameters: Preliminaries, continuity, and differentiability.

Books Recommended :

1. P.Hartman, Ordinary differential equations, John Wiley, 1964.
2. Walter Rudin, Principles of Mathematical Analysis, (3rd edition), McGraw-Hill international editions, 1976.

References :

1. W.T.Reid, Ordinary differential equations, John Wiley & sons, New York,1971.
2. E.A.Coddigton & N.Levinson, Theory of ordinary differential equations, McGraw Hill, NY, 1955.

E-references:

1. Ordinary Differential Equations, Modern Perspective Mohan C Joshi IITBombay http://www.math.iitb.ac.in/~mcj/root.pdf
2. Differential Equations, Paul Dawkins http://tutorial.math.lamar.edu/pdf/DE/DE_Complete.pdf
3. Ordinary Differential Equations-Lecture Notes, Eugen J. Ionascu http://math.columbusstate.edu/ejionascu/papers/diffeqbook.pdf

SEMESTER – II

M 211
MODULE THEORY

Pre-requisites: Basics on rings and fields.(relevant parts of reference [1])

Unit I:
Modules: Basic definitions, direct products and sums, Free modules.

Unit II:
Noetherian rings and modules, Hilbert Basis Theorem, Power series, Associated primes, primary decomposition.

Unit III:
Modules over PID's, decomposition over one endomorphism, Characteristic polynomial, Jordan & Rational canonical forms.

Unit IV:
Semisimplicity: Matrices & Linear maps over non-commutative rings, conditions defining semisimplicity, the Density theorem,

Unit V:
semisimple rings & simple rings .Representations of finite groups.

Book Recommended:

1. Serge Lang : Algebra

Reference Books:

1. I.N.Herstein, Topics in Algebra, Wiley Eastern Ltd., New Delhi, 1975.
2. M.Artin, Algebra, Prentice - Hall of India, 1991.
3. N.Jacobson, Basic Algebra, vols I&II, W.H.Freeman,1980.
4. S.Kumaresan, Linear Algebra, A Geometric Approach, Prentice - Hall of India
5. D.S.Dummit & R.M.Foote, Abstract Algebra, II Ed, John Wiley & Sons, Inc, New York.

M 212

REAL ANALYSIS-II

Pre-requisites: Algebra of sets, σ algebra, Riemann integration

Unit I:

Lebesgue outer measure, measurable sets, a non measurable set

Unit II:

Hausdorff measures on the real line, Hausdorff dimension, Hausdorff dimensions of a Cantor like set.

Unit III:

measurable functions, Littlewoods three principles, a non Borel measurable set, Egoroff's theorem

Unit IV:

the Lebesgue integral of a bounded function over a set of finite measure, the integral of a nonnegative function, the general Lebesgue integral, properties of these integrals, convergence theorems.

Unit V:

Differentiation of monotone functions, functions of bounded variation, differentiation of an integral, absolute continuity, convex functions, the Lp spaces, the Minkowski and Holder inequalities, convergence and completeness, Bounded linear functionals on Lp spaces..

Books Recommended:

1. H.L. Royden, Real Analysis(4th edition), Macmillan Publishing Company, 1993.

References:

1. G. de. Barra, Measure Theory and Integration, Wiley Eastern Limited, 1981.
2. Lebesgue Measure and integration: an introduction, Frank Burk, Wiley Interscienc Publication, 1998.
3. Inder K. Rana, An Introduction to Measure and Integration, Narosa Publishing House, Delhi, 1997.

E-references:

1. http://www.math.dauniv.ac.in/Dr.MaheshNDumaldar.php
2. Review of Lebesgue Measure and Integration, Christopher E. Heil, School of Mathematics Georgia Institute of Technology
   http://people.math.gatech.edu/~heil/handouts/real.pdf
3. Measure Theory and Lebesgue Integration, Joshua H. Lifton
   http://web.media.mit.edu/~lifton/snippets/measure_theory.pdf
4. The Lebesgue Measure and Integral, Mike Klaas
   http://www.cs.ubc.ca/~klaas/research/lebesgue.pdf

M 213
TOPOLOGY – II

Pre-requisites: M113

Unit I:

Compactness. Continuous functions and compact sets. Basic properties of compactness. Compactness and finite intersection property. Sequentially and Countably compact sets.

Unit II:

Local compactness and one-point compactification. Compactness in metric spaces. Equivalence of compactness, Countable compactness and Sequential compactness in metric spaces. Nets.

Unit III:

First and second countable spaces. Lindelof's theorems. Second countability and separability. Countability and product spaces. Separation axioms. T_0, T_1, T_2, T_3, T_4; their characterizatrion and basic properties. Urysohn's lemma.

Unit IV:

Tietze extension theorem. Urysohn (metrization) embedding theorem. Separation axioms and product spaces. The Tychonoff's theorem. Stone-Cech compactification.
Metrization theorems and paracompactness: Local finiteness. The Nagata-Smirnov metrization theorem. Paracompactness. The Smirnov metrization theorem.

Unit V:

The fundamental group and covering spaces : Homotopy of paths. The fundamental group. Covering spaces. The fundamental group of the circle and the fundamental theorem of algebra.

Books Recommended :

1. James R. Munkres, Topology (Second edition), Prentice-hall of India
2. George F. Simmons, Introduction to topology and modern analysis,McGraw Hill Book Company Inc.

References :

1. N. Bourbaki, General topology, Springer-verlag.
2. K.D.Joshi, Introduction to topology, Wiley Eastern.
3. J.L.Kelley, General topology, Affiliated East-West press Pvt Ltd.

E-references:

1. Topology Course Lecture Notes Aisling McCluskey and Brian McMaster http://at.yorku.ca/i/a/a/b/23.htm
2. Notes on Introductory Point-Set Topology, Allen Hatcher http://www.math.cornell.edu/~hatcher/Top/TopNotes.pdf
3. Introduction to Topology, Renzo http://www.math.colostate.edu/~renzo/teaching/Topology10/Notes.pdf
4. Topology Lecture Notes, Thomas Ward, UEA http://www.uea.ac.uk/~h720/teaching/topology/materials/topology.pdf

M 214
COMPLEX ANALYSIS-II

Pre-requisites: Basic Metric space theory: relevant parts of reference [1]

Unit I:
Spaces of analytic functions, Hurwitz's theorem, Montel's theorem,Riemann Mapping theorem, Weierstrass Factorisation theorem.

Unit II: Gamma function & it's properties, Riemann Zeta function, Riemann's functional equation, Runge's theorem and Mittag-Leffler's theorem.

Unit III: Analytic continuation, uniqueness of direct analytic continuation and analytic continuation along a curve, power series method of analytic continuation, Schwartz Reflection Principle, Monodromy theorem and it's consequences.

Unit IV: Harmonic functions on a disk, Dirichlet problem, Green's function.

Unit V: Canonical products, Jensen's formula, order of an entire function, exponent of convergence,Hadamard's factorization theorem, range of an analytic function,Bloch's theorem, The Little Picard theorem, Schottky's theorem, Great Picard theorem.

Books Recommended:

1.J.B.Conway : Functions of one Complex variable, Springer-verlag.
2. S.Ponnusamy : Foundations of Complex Analysis, Narosa Pub, `97

References :

1. Alfohrs : Complex Analysis

E-references:

1. Introduction to Complex Analysis

   http://rutherglen.science.mq.edu.au/wchen/lnicafolder/lnica.html

2. Complex Analysis

   www.umn.edu/~arnold/502.s97/complex.pdf

M 201

DIFFERENTIAL EQUATIONS-II

Pre-requisites: M101

Unit I:
Poincare- Bendixson theory: Autonomous systems, Umlanfsatz, index of a stationary point, Poincare- Bendixson theorem, stability of periodic solutions,

Unit II:
rotation points, foci, nodes and saddle points. Linear second order equations : Preliminaries, Basic facts, Theorems of Sturm,

Unit III:
Sturm-Liouville boundary value problems, Number of zeros,

Unit IV:
Nonoscillatory equations and principal solutions, Nonoscillation theorems.

Unit V:
Use of Implicit function and fixed point theorems : Periodic solutions, linear equations, nonlinear problems.

Books recommended :

1. P.Hartman, Ordinary differential equations, John Wiley, 1964.

References :

1. W.T.Reid, Ordinary differential equations, John Wiley & sons, New York,1971.
2. E.A.Coddigton & N.Levinson, Theory of ordinary differential equations, McGraw Hill, NY, 1955.

E-references:

1. Ordinary Differential Equations, Modern Perspective Mohan C Joshi IITBombay

   http://www.math.iitb.ac.in/~mcj/root.pdf

2. Differential Equations, Paul Dawkins

   http://tutorial.math.lamar.edu/pdf/DE/DE_Complete.pdf

3. Ordinary Differential Equations-Lecture Notes, Eugen J. Ionascu

   http://math.columbusstate.edu/ejionascu/papers/diffeqbook.pdf

SEMESTER – III

M 311

INTEGRATION THEORY

Pre-requisites: Lebesgue Measure theory [1]

Unit I:

Measure spaces, Measurable functions, Integration, Convergence theorems.

Unit II: Signed measures, The Radon-Nikodym theorem, Lebesgue decomposition, L^P spaces, Riesz representation theorem.

[1] Chapter 11

Unit III: Outer measure and measurability, The extension theorem, Lebesgue- Steiltjes integral, Product measures, Fubini's theorem.

[1] Chapter 12, Sections 1,2,3,4.

Unit IV: Baire sets, Baire Measure, Continuous functions with compact support, Regularity of measures on locally compact spaces.

Unit V: Integration of continuous functions with compact support, Riesz- Markoff theorem.

[1] Chapter 13.

Recommanded Books :

1. H.L. Royden, Real Analysis, Mc millan Pub. Co. Inc. New York, 4th Edition, 1993.
2. G.de.Barra., Measure Theory and Integration, Wiley Eastern Limited, 1981
3. Inder K. Rana. An introduction to Measure & Integration Narosa Pub. House, Delhi,1997.
4. P.K. Jain, N.P. Gupta, Lebesgure Measure and Interation New Age International (P) Ltd., New Delhi, 1986.

E-references:

1. Notes on measure and integration in locally compact – Mathematics
   http:/math.berkeley.edu/~arveson/Dvi/rieszMarkov.pdf

M 312

FUNCTIONAL ANALYSIS

Pre-requisites: Metric spaces, compactness, connectedness.

Unit I:
Completion of a metric space, Normed linear spaces. Banach spaces and examples. Quotient space of normed linear space and its completeness.

Unit II:
Equivalent norms. Riesz lemma, basic properties of finite dimensional normed linear space and compactness. Weak convergence and bounded.

Unit III:
linear transformations, normed linear spaces of bounded linear transformations, dual spaces with examples. Open mapping and closed graph theorems. Uniform boundedness theorem and some of its consequences, the Hahn-Banach theorem.

Unit IV:
Reflexive spaces. Weak sequential compactness.

Unit V:
Inner product spaces. Hilbert spaces. Orthonormal sets. Bessel's inequality. Complete orthonormal sets and Parseval's identity. Structure of Hilbert spaces. Projection theorem, Riesz representation theorem. Adjoint of an operator on a Hilbert space. Reflexivity of Hilbert spaces. Self-adjoint operators, positive, projection, normal and unitary operators.

Recommended Books :

1. H.L. Royden, Real Analysis, Macmillan Publishing Co. Inc. New York, 4th Edition, 1993.
2. G.F. Simmons, Introduction to Topology and Modern Analysis, McGraw- Hill Book Company, New York, 1963.
3. E. Kreyszig, Introductory Functional Analysis with Applications, John Wiley & Sons. New York, 1978
4. B.V. Limaye, Functional Analysis, New Age Intergration (P) Ltd., 1996

E-references:

1. An introduction to some aspects of functional analysis, Stephen Semmes, Rice University : http://math.rice.edu/~semmes/fun2.pdf
2. http://www.math.dauniv.ac.in/Dr.MaheshNDumaldar.php

M 313

PARTIAL DIFFERENTIAL EQUATIONS

Unit I:

Examples of PDE. Classification. Transport Equation-Initial Value Problem. Non-homogeneous Equation.

Unit II:

Laplace's Equation - Fundamental Solution, Mean Value Formulas, Properties of Harmonic Functions, Green's Function,Energy Methods. Heat Equation- Fundamental Solution, Mean Value Formula, Properties of Solutions, Energy Methods.

Unit III:

Wave Equation-Solution by Spherical Means, Non- homogeneous Equations, Energy Methods.

[1] Chapter 1 Art. 1.1, 1.2, Chapter. 2

Unit IV:

Nonlinear First Order PDE-Complete Integrals, Envelopes, Characteristics,

Unit V:

Hamilton-Jacobi Equations (Calculus of Variations, Hamilton's ODE, Legendre Transform, Hopf-Lax Formula, Weak Solutions, Uniqueness),

[1] Chapter. 3 Art. 3.1 to 3.3

Recommended Books:

1. L.C. Evans, Partial Differential Equations, Graduate Studies in Mathematics, Volume 19, AMS, 1998.

Reference Books:

1. I. N. Sneddon, Elements of Partial Differential Equations, Mc Graw-Hill Book Company, 1985.
2. F. John, Partial Differential Equations, Third Edition, Narosa Publishing House, New Delhi, 1979.
3. P. Prasad and R. Ravidran, Partial Differential Equations, New Age International (P) Limited, Publishers, 1985.

E-references:

1. Partial Differential Equations MA 3132 Lecture Notes, B. Neta
   http://www.math.nps.navy.mil/~bneta/pde.pdf
2. Notes for Partial Differential Equations, Kuttler
   http://www.math.byu.edu/~klkuttle/547notesB.pdf

M 301

THEORY OF LINEAR OPERATORS-I

Pre-requisites: Basic linear algebra and basic functional analysis.

Unit I:

Spectral theory of normed linear spaces, resolvent set and spectrum, spectral properties of bounded linear operators, properties of resolvent and spectrum.

[1] Chapter 7

Unit II:

spectral mapping theorem for polynomials, spectral radius of bounded linear operator on a complex Banach space, elementary theory of Banach Algebras. [1] Chapter 7

Unit III:

Basic properties of compact linear operators. [1] Chapter 8

Unit IV:

Behaviour of Compact linear operators with respect to solvability of operator equations, Fredholm type theorems, Fredholm alternative theorem, Fredholm alternative for integral equations. [1] Chapter 8

Unit V:

Spectral properties of bounded self-adjoint linear operators on a complex Hilbert space, positive operators, Monotone sequence theorem for bounded self-adjoint operators on a complex Hilbert space, square roots of a positive operator, projection operators.

[1] Chapter 9, Sec 9.1-9.6

Recommended Book:

1. E.Kreyszig, Introductory Functional Analysis with applications, John-Wiley & Sons, New York, 1978.

Reference Books:

1. N.Dunford & J.T.Schwartz,Linear operators-3 parts, Interscience Wiley, New York, 1958-71.
2. P.R. Halmos, Introduction to Hilbert spaces and the theory of spectral multiplicity, second edition, Chelsea Pub. Co., N.Y. 1957.
3. P. R. Halmos, A Hilbert space problem book, D. Von Nostrand company Inc., 1967.

M 302

Linear Programming - I

Pre-requisites: Finite dimensional vector spaces, Linear transformations, Linear system of equations, basic solutions

Unit I:

Inverse of matrix by partition, product form of the inverse, basis to basis lemma, lines & hyperplanes, Convex sets and hyperplanes, polyhedral sets, extreme points, faces, directions and extreme directions, Decomposition theorem for polyhedra, Farkas' lemma.

Unit II:

Theory of simplex method, reduction of any feasible solution to a basic feasible solution, improving a basic feasible solution, unbounded solutions, optimality conditions, alternate optima, extreme points and basic feasible solutions,

Unit III:

computational aspects of the simplex method, initial basic feasible solution, inconsistency and redundancy, review of the simplex method, Big M method, two phase method

Unit IV:

resolution of degeneracy, Charne's perturbation method, Blande's rule, Revised simplex method, the simplex method for bounded variables.

Unit V:

Network Analysis: Shortest path problem, minimum spanning tree problem, Maximum flow problem, Minimum cost flow problem, Network simplex method.

Recommended Books:

1. G. Hadley, Linear programming, Narosa Publishing House, 1995.
2. Mokhtar S. Bazaraa, John J. Jarvis, Hanis D. Sherali, Linear Programming And Network Flows, 2nd Ed, Wiley-India, 2008
3. Schrijver,A.: Theory of Linear and Integer Programming, J. Wiley, 1986

Reference Books:

1. Dantzig G., Thapa M. Linear programming. Vol.1.. Introduction, Springer,1997
2. G.B. Dantzig, M. Thapa: Linear Programming 2: Theory and Extensions, Springer Verlag, 2003
3. G.Hadley, Linear Algebra, Addison – Wesley Pub. Co. Read. Mass. 1961
4. Nemhauser G.L., Wolsey L.A., Integer and combinatorial optimization, Wiley, NewYork, 1988
5. Chvatal V., Linear programming, Freeman, NewYork, 1983
6. Vanderbei R.J., Linear programming: Foundations and extensions, Kluwer Academic Publishers, Boston, MA, 1996

E-references:

1. http://www.math.dauniv.ac.in/Dr.MaheshNDumaldar.php
2. Activity Analysis of Production and Allocation, Proceedings of a Conference, Tjalling C. Koopmans
3. National Programme on Technology Enhanced Learning.(Mathematics)

SEMESTER – IV

M 411
MECHANICS

Unit I:

Generalized coordinates. Holonomic and Non-holonomic Systems. Scleronomic and Rheonomic Systems. Generalized potential.

Unit II:

Lagrange's equations of first kind. Lagrange's equations of second kind. Uniqueness of solution. Energy equation for conservative fields. Hamilton's variables. Donkin's theorem. Hamilton canonial equations. Cyclic coordinates. Routh's equations.

Unit III:

Motivating problems of calculus of variations, Shortest distance. Minimum surface of revolution. Brachistochrone problem. Isoperimetric problem. Geodesic. Fundamental lemma of calculus of variations. Euler's equation for one dependent function and its generalization to (i) `n' dependent functions (ii) higher order derivatives. Conditional extremum under geometric constraints and under integral constraints.

Unit IV:

Hamilton's principle, Principle of least action.

[2] Art. 1-6 & relevant parts of 8, 11-14, 16,20, [3] Relevant portion for Calculus of variations.

Unit V:

Poincare Cartan integral invariant. Whittaker's equations. Jacobi's equations. Statement of Lee Hwa Chung's theorem. Hamilton-Jacobi equation. Jacobi theorem. Method of seperation of variables. Lagrange brackets. Poisson's bracket. Poisson's identity. Jacobi-Poisson Theorem. Condition of canonical character of a transformation in terms of Lagrange brackets and Poisson brackets. Invarience of Lagrange brackets and Poisson brackets under canonial transformations.

[2] Art. 15, 18, 20, 22, 24-27, 30, 32.

Books Recommended :

1. F. Gantmacher, Lectures in Analytic Mechanics, MIR Publishers, Moscow, 1975.

Reference Books:

1. H. Goldstein, Classical Mechanics (2nd Edition), Narosa Publishing House, New Delhi.
2. Narayan Chandra Rana and Pramod Sharad Chandra Joag, Classical Mechanics, Tata McGraw Hill, 1991.
3. Louis N. Hand and Janet D. Finch, Analytical Mechanics, Cambridge University Press, 1998.

M 401

THEORY OF LINEAR OPERATORS – II

Pre-requisites: M 301

Unit I:

Spectral family of a bounded self-adjoint linear operator and it's properties, spectral representation of bounded self-adjoint linear operators, spectral theorem

[1] Chapter 9, Sec 9.7-9.11

Unit II:

Unbounded linear operators in Hilbert space, Hellinger-Toepliz theorem. [1] Chapter 10

Unit III:

Hilbert adjoint operators, Symmetric and self-adjoint linear operators, closed linear operators and closures, spectrum of an unbounded self-adjoint linear operator.

[1] Chapter 10

Unit IV:

spectral theorem for unitary and self adjoint linear operators. [1] Chapter 10

Unit V:

Multiplication operator and Differentiation operator. [1] Chapter 10

Recommended Book:

1. E.Kreyszig, Introductory Functional Analysis with applications, John-Wiley & Sons, New York, 1978.

Reference Book:

1. N.Dunford & J.T.Schwartz,Linear operators-3 parts, Interscience Wiley, New York, 1958-71.

M 402

Linear Programming –II

Pre-requisites: M401

Unit I:

Duality theory, weak and strong duality theorems, Complementary slackness, dual simplex method, primal dual algorithm, Integer programming, the KKT conditions.

Unit II:

Transportation problems, properties of the activity matrix of a transportation problem, simplification of the simplex method to the transportation problem, bases in a transportation problem, the stepping stone algorithm, resolution of degeneracy, determination of an initial basic feasible solution, alternative procedure for computing z_{ij} -c_{ij} using duality(u-v method).

Unit III:

Assignment problems, reduced cost coefficient matrix, the Hungarian method, Konig – Evergary theorem, The Birkoff –von Neumann theorem.

Unit IV:

Sensitivity analysis, the Dantzig-Wolf decomposition, Game theory and linear programming, Two person zero sum games, Games with mixed strategies, Graphical solution, Solution by linear programming.

Unit V:

Applications: Optimal product mix and activity levels, Petroleum refinery operations, Blending problems, Economic interpretation of dual linear programming problems, Input output analysis, Leotief systems.

Recommended Books:

1. G. Hadley, Linear programming, Narosa Publishing House, 1995.
2. Mokhtar S. Bazaraa, John J. Jarvis, Hanis D. Sherali, Linear Programming And Network Flows, 2Nd Ed, Wiley-India, 2008
3. Schrijver,A.: Theory of Linear and Integer Programming, J. Wiley, 1986

Reference Books:

1. Dantzig G., Thapa M. Linear programming. Vol.1.. Introduction, Springer,1997
2. G.B. Dantzig, M. Thapa: Linear Programming 2: Theory and Extensions, Springer Verlag, 2003
3. G.Hadley, Linear Algebra, Addison – Wesley Pub. Co. Read. Mass. 1961
4. Nemhauser G.L., Wolsey L.A., Integer and combinatorial optimization, Wiley, NewYork, 1988
5. Chvatal V., Linear programming, Freeman, NewYork, 1983
6. Vanderbei R.J., Linear programming: Foundations and extensions, Kluwer Academic Publishers, Boston, MA, 1996

E-references:

1. http://www.math.dauniv.ac.in/Dr.MaheshNDumaldar.php
2. Activity Analysis of Production and Allocation, Proceedings of a Conference, Tjalling C. Koopmans.
3. National Programme on Technology Enhanced Learning.(Mathematics)

M 403

HOMOTOPY THEORY

Pre-requisites: M113 & M213

Unit I:

The Fundamental Group, Homotopic Paths and the Fundamental Group.

Unit II:

The Covering Homotopy Property for S^{1}, Examples of Fundamental Groups.

[1] Chapter 4.

Unit III:

Covering Spaces, The Definition and Some Examples, Basic Properties of Covering Spaces, Classification of Covering Spaces, Universal Covering Spaces, Applications. [1] Chapter 5.

Unit IV:

The Higher Homotopy Groups, Equivalent Definitions of $\pi_n(X, x_0)$, Basic Properties and Examples.

Unit V:

Homotopy Equivalence, Homotopy Groups of Spheres.[1] Chapter 6.

Recommended Book:

1. F. H. Croom : Basic Concepts of Algebraic Topology, Springer-Verlag New York.
2. W.S. Massey : Algebraic Topology, Springer -Verlag.
3. E.H. Spanier : Algebraic Topology : Mc Graw – Hill Book Company.

M 404

TOPICS IN RING THEORY

Pre-requisites: Basic definitions and results concerning rings and fields.

Unit I:

Rings and Ring Homomorphisms, Ideals Quotient Rings, Zero Divisors, Nilpotent Elements, Units.

Unit II:

Prime Ideals and Maximal Ideals, Niltradial & Jacobson Radial Operations an Ideals, Extension & Contraction.

Unit III:

Modules,Operation on Submodules, Direct Sum and Product of Modules, Restriction and Extension of Scalars.

Unit_IV:

Tensor product of modules, basic properties ,Exactness Properties of Tensor Product, Algebras & Tensor Product of Algebras.

Unit-V:

Rings and Modules of Fractions, Local Properties Extended and Contracted Ideals in Ring of Fractions. (with Emphasis an Exercise) [1 chapter 1 to 3]

Books Recommended :

1. Introduction to Commutative Algebra, Atiyah & I.G. Macdonald,
   Addison – Wesley Pub. Co

E-references:

1. **Commutative Algebra Notes** Branden Stone
   www.math.bard.edu/~bstone/commalg-**notes**/
2. **Commutative Algebra** Lecture **Notes** - Tata Institute of Fundamental
   www.math.tifr.res.in/~anands/CA-Lecture%20**notes**.pdf

M 405

ALGEBRAIC TOPOLOGY

Pre-requisites: M113 & M213

UNIT I :

Deformation retracts and homotopy type. Fundamental group of S for $n > 1$, and some surfaces. The Jordan seperation theorem, the Jordan curve theorem, Imbedding graphs in plane.

[1] Chapter 9, sections 58 to 60 & Chapter 10, sections 61, 63 and 64.

UNIT II :

Free product of groups, Free groups, The Siefert- van Kampen theorem and its applications. Classification of surfaces : Fundamental groups of surfacees, Homology of surfaces, Cutting and pasting, Construction of Compact surfaces, The classification theorrem.

[1] Chapter 11, sections 68 to 73 & Chapter 12, sections 74 to 78.

Unit III :

Equivalence of covering spaces, Covering transformations, The universal covering space, and its existence.: Homology groups of a simplicial complex : Simplicial complexes and simplicial maps, Homology groups, Homology groups of surfaces, Zero-dimensional homology, The homology of a cone, Relative homology, Homomorphisms induced by simplicial maps, Chain complexes and acyclic carriers. [1] Chapter 13. [2] Chapter 1, Sections 1 to 9, 12 & 13.

UNIT IV :

Relative homology : The exact homology sequence, Mayer-vietoris sequences, The Eilenberg-Steenrod axioms (without proofs). The singular homology groups, The axioms for Singular theory (without proofs), Mayer-Vietoris sequences, The isomorphism between simplicial and singular homology, CW complexes, The homology of CW complexes and application to Projective spaces and Lens spaces.

[2] Chapter 3, Sections 23 to 28 (relevant portions)

Chapter 4, Sections 29 to 34 & 37 to 40 (relevant portions)

UNIT V :

Cohomology : The Hom functor, Simplicial cohomology groups, Relative cohomology, The cohomology of frre chain complexes, The cohomology of CW complexes, Cup products, Cohomology ring of surfaces.

[2] Chapter 5, Sections 41 to 49.

Books recommended :

1. J.R. Munkres, Topology, Second edition, Prentice-Hall of India, 2000.
2. J.R. Munkres, Elements of Algebraic topolgy, Addison-Wesley Publishing company, 1984.

M 406

Analytic Number Theory

Unit I: Characters of finite abelian groups, The character group, Dirichlet characters, Sums involving Dirichilet characters, Dirichlet's theorem on primes in arithmetic progressions. [1] Chapter 6, sections 6.5 to 6.10, Chapter 7

Unit II: Dirichlet series and Euler products, the function defined by Dirichlet series, The half-plane of convergence of a Dirichlet series, Integral formula for the coefficients of Dirichlet series, etc. [1] Chapter 11

Unit III: Properties of the gamma functions, Integral representations of Hurwitz zeta functions, Analytic continuation of hurwitz zeta functions, Functional equation for the Riemann zeta function and properties of Riemann zeta functions etc. [1] Chapter 12

Unit IV: Analytic proof of prime number theorem. [1] Chapter 13

Unit V: Geometric representation of partitions, Generating functions of partitions, Euler's pentagonal number theorem, Euler's recursion formula for p(n), Jacobi's triple product identity, The partition identity of Ramanujan. [1] Chapter 14

Book Recommneded:

1. T. M. Apostol, Introduction to Analytic Number Theory, Narosa Pub, House, 1989.

M 407

Abstract Harmonic Analysis

Unit I : Definition of a topological group and its basic properties. Subgroups and quotient groups. Product groups & projective limits. [1], Sections 4,5,6 of Chapter Two.

Unit II : Properties of topological groups involving connectedness. Invariant pseudo-metrics and separation axioms. Structure theory for compact and locally compact Abelian groups. Some special locally compact Abelian groups. [1], Sections 7,8,9,10 of Chapter Two.

Unit III : The Haar integral. Haar Measure. Invariant means defined for all bounded functions. Invariant means of almost periodic functions. [1], Chapter Four.

Unit IV : Convolutions, Convolutions of functions and measures. Elements of representation theory. Unitary representations of locally compact groups. [1], Chapter Five.

Unit V : The character group of a locally compact Abelian group and the duality theorem. [1], Sections 23,24 of Chapter Six.

Recommended Book :

1. Edwin Hewitt and Kenneth A. Ross, Abstract Harmonic Analysis-I, Springer-Verlag, Berlin, 1993.

Reference :

1. Lynn H. Loomis, An introduction to abstract harmonic analysis, D. Van Nostrand Co. Princeton.

School of Mathematics, DAVV, Indore

Taking into consideration the recent advances in different areas of mathematics, the board of studies in Mathematics, after discussions with experts, has revised the syllabus of M.Sc./M. A. Mathematics course.

Aims:

1. Strengthening the logical reasoning which is the main ingredient to understand mathematical concepts.
2. Create more interest in the subject and motivate students for self learning.
3. Developing the mathematical skills among the students and preparing them to take up a career in research.

Objectives:

1. To make students understand the techniques of proof in Mathematics and apply suitable techniques to tackle problems.
2. To inculcate the habit of making observations and experimentation and arrive at the final result.
3. Make student acquire the communication skill to present technical Mathematics so as to take up a career in Teaching Mathematics at various levels including schools, colleges, universities, etc.

General e-references:

1. National Programme on Technology Enhanced Learning.(Mathematics)

   http://www.nptelvideos.com/mathematics/

2. Mathematics Video Lectures

   http://freevideolectures.com/Subject/Mathematics

3. MIT Open Course Ware

   http://ocw.mit.edu/courses/audio-video-courses/

e-references pertinent to each course are given at the end of the syllabus of the course.

SCHEME OF EXAMINATION
M.A. /M.Sc. Mathematics.

Semester I

CODE	SUBJECT	L	T	C
M 111	Field theory	4	--	4
M 112	Real Analysis-I	4	--	4
M 113	Topology-I	4	--	4
M 114	Complex Analysis-I	4	--	4
M 101	Differential Equations-I	4	--	4
	Viva-Voce			4

Contact hours	:	20 per week
Valid credits	:	20
L	:	Lecture
T	:	Tutorial
C	:	Credits

* The following notation comprising of three digits is used while numbering the courses.

1. The first digit refers to the semester number i.e. 1,2,3, and 4.
2. The second digit 1 refers to a core course and the second digit 0 refers to an optional course.
3. The third digit refers to the serial number of the course.

SCHEME OF EXAMINATION

M.A. /M.Sc. Mathematics

Semester II

CODE	SUBJECT	L	T	C
M 211	Advanced Abstract Algebra	4	--	4
M 212	Real Analysis-II	4	--	4
M 213	Topology-II	4	--	4
M 214	Complex Analysis-II	4	--	4
M 201	Differential Equations-II	4	--	4
	Viva-Voce			4

Contact hours	:	20 per week
Valid credits	:	20
L	:	Lecture
T	:	Tutorial
C	:	Credits

* The following notation comprising of three digits is used while numbering the courses.

1. The first digit refers to the semester number i.e. 1,2,3, and 4.
2. The second digit 1 refers to a core course and the second digit 0 refers to an optional course.
3. The third digit refers to the serial number of the course.

SCHEME OF EXAMINATION

M.A. /M.Sc. Mathematics

Semester III

CODE	SUBJECT	L	T	C
M 311	Integration Theory	4	-	4
M 312	Functional Analysis	4	-	4
M 313	Partial Differential Equations	4	-	4
M 301	Theory of Linear Operators-I	4	-	4
M 302	Linear Programming-I	4	-	4
M305	Mathematical Modelling-I	3		3
	Viva-Voce			4

Contact hours	:	23 per week
Valid credits	:	23
L	:	Lecture
T	:	Tutorial
C	:	Credits

* The following notation comprising of three digits is used while numbering the courses.

1. The first digit refers to the semester number i.e. 1,2,3, and 4.
2. The second digit 1 refers to a core course and the second digit 0 refers to an optional course.
3. The third digit refers to the serial number of the course.
4. M305 is an elective generic course.

SCHEME OF EXAMINATION

M.A. /M.Sc. Mathematics

Semester IV

CODE	SUBJECT	L	T	C
M 411	Mechanics	4	-	4
M 401	Theory of Linear Operators - II	4	-	4
M 402	Linear Programming -II	4	-	4
M 403	Homotopy Theory	4	-	4
M 404	Topics In Ring Theory	4	-	4
M405	Mathematical Modelling-II	3	--	3
	Viva-Voce			4

Contact hours	:	23 per week
Credits	:	23
L	:	Lecture
T	:	Tutorial
C	:	Credits

* The following notation comprising of three digits is used while numbering the courses.

1. The first digit refers to the semester number i.e. 1,2,3, and 4.
2. The second digit 1 refers to a core course and the second digit 0 refers to an optional course.
3. The third digit refers to the serial number of the course.
4. M405 is an elective generic course.

CORE COURSES

Semester I

M 111 Field theory
M 112 Real Analysis-I
M 113 Topology-I
M 114 Complex Analysis-I

Semester II

M 211 Advanced Abstract Algebra
M 212 Real Analysis-II
M 213 Topology-II
M 214 Complex Analysis-II

Semester III

M 311 Integration Theory
M 312 Functional Analysis
M 313 Partial Differential Equations

Semester IV

M 411 Mechanics

ELECTIVE COURSES(Discipline Centric)

Semester I

CODE	SUBJECT
M 101	Differential Equations-I
M 102	Advanced Discrete Mathematics-I
M 103	Differential Geometry of Manifolds-I

Semester II

CODE	SUBJECT
M 201	Differential Equations-II
M 202	Advanced Discrete Mathematics-II
M 203	Differential Geometry of Manifolds-II

Semester III

CODE	SUBJECT
M 301	Theory of Linear Operators-I
M 302	Linear Programming-I
M 303	Pragramming in C – Theory & Practical
M 304	Mathematics of Finance & Insurance-I

Semester IV

CODE	SUBJECT
M 401	Theory of Linear Operators - II
M 402	Linear Programming-II
M 403	Homotopy Theory
M 404	Topics In Ring Theory
M 405	Algebraic Topology
M 406	Analytical Number Theory
M 407	Abstract Harmonic Analysis
M 408	Mathematics of Finance & Insurance-II

* Those electives will be offered for which expertise is available in the department.

ELECTIVE COURSE(Generic)

M305 Mathematical Modelling-I
M405 Mathematicsl Modelling-II

SYLLABUS

M.A./M.Sc. MATHEMATICS

SEMESTER I

M 111 Field theory

M 112 Real Analysis-I

M 113 Topology-I

M 114 Complex Analysis-I

M 101 Differential Equations-I

SEMESTER II

M 211 Module Theory

M 212 Real Analysis-II

M 213 Topology-II

M 214 Complex Analysis-II

M 201 Differential Equations-II

SEMESTER III

M 311 Integration Theory

M 312 Functional Analysis

M 313 Partial Differntial Equations

M 301 Theory of Linear Operators-I

M 302 Linear Programming-I

SEMESTER IV

M 411 Mechanics

M 401 Theory of Linear Operators - II

M 402 Linear Programming -II

M 403 Homotopy Theory

M 404 Topics in Ring Theory

Course Plan: Each course has five units and each unit shall be covered in three weeks on average.

SEMESTER - I

M 111
FIELD THEORY

Pre-requisites: Basics on rings and fields.(relevant parts of reference [1])

Unit I:
Finite & Algebraic extensions, Algebraic closure,

Unit II:
splitting fields and normal extensions, separable extensions,

Unit III:
Finite fields, Primitive elements and purely inseparable extensions.

Unit IV:
Galois extensions, examples and applications,

Unit V:
Roots of unity, Linear independence of characters, cyclic extensions, solvable & radical extensions.

Book Recommended:

1. Serge Lang : Algebra

Reference Books:

1. I.N.Herstein, Topics in Algebra, Wiley Eastern Ltd., New Delhi, 1975.
2. M.Artin, Algebra, Prentice - Hall of India, 1991.
3. N.Jacobson, Basic Algebra, vols I&II, W.H.Freeman,1980.
4. S.Kumaresan, Linear Algebra, A Geometric Approach, Prentice - Hall of India, 2000.
5. D.S.Dummit & R.M.Foote, Abstract Algebra, II Ed, John Wiley & Sons, Inc, New York.

E-references:

1. Notes on Galois Theory, Sudhir R. Ghorpade
   Department of Mathematics, Indian Institute of Technology, Bombay 400 076
   http://www.math.iitb.ac.in/~srg/Lecnotes/galois.pdf

2. Galois Theory, Dr P.M.H. Wilson.
   http://www.jchl.co.uk/maths/Galois.pdf

M 112
REAL ANALYSIS-I

Pre-requisites: Chapters 1 to 5 of reference [1]

Unit I:

The Riemann-Stieltjes Integral Definition and existence of the integral, properties of the integral, integration and differentiation, integration of vector-valued functions, rectifiable curves.

Unit II:

Sequences and Series of Functions Rearrangements of terms of a series, Riemann theorem, pointwise and uniform convergence, Cauchy criterion for uniform convergence, Weiestrass M-test, uniform convergence and continuity, uniform convergence and integration.

Unit III:

Uniform convergence and differntiation, equicontinuous families of functions, the Stone-Weierstrass Theorem, uniform convergence and Riemann-Stieltjes integral,

Unit IV:

Abels test for uniform convergence, Dirichlet's test for uniform convergence.
power series, Abel's theorem.

Unit V:

Functions of Several Variables, derivatives in an open subset of R^n, chain rule, partial derivatives, interchange of the order of differentiation, derivatives of higher orders, inverse function theorem, implicit function theorem, Jacobians, differentiation of integrals, Taylor's theorem, extremum problems with constraints, Lagrange's multiplier method.

Books Recommended:

1. Walter Rudin, Principles of Mathematical Analysis(3rd edition), McGraw-Hill international editions, 1976.
2. T.M. Apostol, Mathematical Analysis(2nd edition), Narosa Publishing House, New Delhi, 1989.

Reference Books:

1. Walter Rudin, Real & Complex Analysis, Tata McGraw-Hill Publishing Co. Ltd., New Delhi, 1966.
2. H.L. Royden, Real Analysis(4th edition), Macmillan Publishing Company, 1993.

M 113
TOPOLOGY – I

Unit I: (Pre-requisites)
Relations,Countable and uncountable sets. Infinite sets and the Axiom of choice. Cardinal numbers and their arithmetic. Schroeder-Bernstein theorem. Cantor's theorem and continuum hypothesis. Zorn's lemma. Well-ordering theorem.

Unit II:
Topological spaces. The order topology. Product topology on X x Y. Bases and subbases. Subspaces and relative topology.

Unit III:
Closed sets and limit points. Closure of a set. Dense subsets. Interior, exterior and boundary of a subset.

Unit IV:
Continuous Functions and homeomorphisms. The product topology. The metric topology. The quotient topology

Unit V:
Connected spaces. Connectedness on the real line. Components. Locally connected spaces. Connectedness and product spaces

Books Recommended :

1. James R. Munkres, Topology (Second edition), Prentice-hall of India
2. George F. Simmons, Introduction to topology and modern analysis, McGraw Hill Book Company Inc.

References :

1. N. Bourbaki, General topology, Springer-verlag.
2. K.D.Joshi, Introduction to topology, Wiley Eastern.
3. J.L.Kelley, General topology, Affiliated East-West press Pvt Ltd.

E-references:

1. Topology Course Lecture Notes Aisling McCluskey and Brian McMaster
   http://at.yorku.ca/i/a/a/b/23.htm
2. Notes on Introductory Point-Set Topology, Allen Hatcher
   http://www.math.cornell.edu/~hatcher/Top/TopNotes.pdf
3. Introduction to Topology, Renzo
   http://www.math.colostate.edu/~renzo/teaching/Topology10/Notes.pdf
4. Topology Lecture Notes, Thomas Ward, UEA
   http://www.uea.ac.uk/~h720/teaching/topology/materials/topology.pdf

M 114
COMPLEX ANALYSIS-I

Pre-requisites:
Basic Metric space theory: relevant parts of reference [1]

Unit I: Algebra of complex numbers, geometric aspects like equations to straight lines, circles, analytic functions, exponential ,trigonometric, hyperbolic functions, Branches of many valued functions with special reference to arg z, log z,and complex exponents.

Unit II:
Complex integration, Cauchy 's Theorem , Cauchy's Integral formula, Higher ordered derivatives, Morera's theorem, Liouville's theorem, Fundamental theorem of algebra.

Unit III:
Taylor's theorem, Maximum Modulus Principle, Schwarz Lemma.

Unit IV:
Isolated singularities, Meromorphic functions, Laurent's series, Argument Principle, Rouche's theorem.

Unit V:
Residues, Cauchy's Residue theorem, evaluation of integrals, , their properties and classification, definitions and examples of conformal mappings, Hadamard three circles theorem.

Books Recommended:

1.J.B.Conway : Functions of one Complex variable, Springer-verlag.
2. S.Ponnusamy : Foundations of Complex Analysis, Narosa Pub, `97

References :
1. George F. Simmons, Introduction to topology and modern analysis, McGraw Hill Book Company Inc.
2. Alfohrs : Complex Analysis

E-references:

1. Introduction to Complex Analysis
   http://rutherglen.science.mq.edu.au/wchen/lnicafolder/lnica.html

2. Complex Analysis
   www.umn.edu/~arnold/502.s97/complex.pdf

M 101
DIFFERENTIAL EQUATIONS-I

Pre-requisites: Chapters 1 to 5 of reference [2]

Unit I:
Initial value problems and the equivalent integral equation, mth order equation in d-dimensions as a first order system, concepts of local existence, existence in the large and uniqueness of solutions with examples. Bassic theorems: Ascoli- Arzela theorem, a theorem on convergence of solutions of a family of initial value problems. Picard-Lindel of theorem, Peano's existence theorem and corollary

Unit II:
Maximal interval of existence, Extension theorem and corollaries, Kamke's convergence theorem, Knesser's theorem. (Statement only) Differential inequalities and uniqueness : Gronwall's inequality, Maximal amd minimal solutions, Differential inequalities.

Unit III:
A theorem of Wintner, Uniqueness theorems, Nagumo's and Osgood's criteria.Egres points and Lyapunov functions, Successive approximations.

Unit IV:
Linear differential equations : Linear systems, Variation of constants, reduction to smaller systems, Basic inequalities, constant coefficients.

Unit V:
Floquet theory, adjoint systems, Higher order equations. Dependence on initial conditions and parameters: Preliminaries, continuity, and differentiability.

Books Recommended :
1. P.Hartman, Ordinary differential equations, John Wiley, 1964.
2. Walter Rudin, Principles of Mathematical Analysis, (3rd edition), McGraw-Hill international editions, 1976.

References :

1. W.T.Reid, Ordinary differential equations, John Wiley & sons, New York,1971.
2. E.A.Coddigton & N.Levinson, Theory of ordinary differential equations, McGraw Hill, NY, 1955.

E-references:

1. Ordinary Differential Equations, Modern Perspective Mohan C Joshi IITBombay http://www.math.iitb.ac.in/~mcj/root.pdf
2. Differential Equations, Paul Dawkins http://tutorial.math.lamar.edu/pdf/DE/DE_Complete.pdf
3. Ordinary Differential Equations-Lecture Notes, Eugen J. Ionascu http://math.columbusstate.edu/ejionascu/papers/diffeqbook.pdf

SEMESTER – II

M 211
MODULE THEORY

Pre-requisites: Basics on rings and fields.(relevant parts of reference [1])

Unit I:
Modules: Basic definitions, direct products and sums, Free modules.

Unit II:
Noetherian rings and modules, Hilbert Basis Theorem, Power series, Associated primes, primary decomposition.

Unit III:
Modules over PID's, decomposition over one endomorphism, Characteristic polynomial, Jordan & Rational canonical forms.

Unit IV:
Semisimplicity: Matrices & Linear maps over non-commutative rings, conditions defining semisimplicity, the Density theorem,

Unit V:
semisimple rings & simple rings .Representations of finite groups.

Book Recommended:

1. Serge Lang : Algebra

Reference Books:

1. I.N.Herstein, Topics in Algebra, Wiley Eastern Ltd., New Delhi, 1975.
2. M.Artin, Algebra, Prentice - Hall of India, 1991.
3. N.Jacobson, Basic Algebra, vols I&II, W.H.Freeman,1980.
4. S.Kumaresan, Linear Algebra, A Geometric Approach, Prentice - Hall of India
5. D.S.Dummit & R.M.Foote, Abstract Algebra, II Ed, John Wiley & Sons, Inc, New York.

M 212

REAL ANALYSIS-II

Pre-requisites: Algebra of sets, σ algebra, Riemann integration
Unit I:
Lebesgue outer measure, measurable sets, a non measurable set

Unit II:
Hausdorff measures on the real line, Hausdorff dimension, Hausdorff dimensions of a Cantor like set.

Unit III:
measurable functions, Littlewoods three principles, a non Borel measurable set, Egoroff's theorem

Unit IV:
the Lebesgue integral of a bounded function over a set of finite measure, the integral of a nonnegative function, the general Lebesgue integral, properties of these integrals, convergence theorems.

Unit V:
Differentiation of monotone functions, functions of bounded variation, differentiation of an integral, absolute continuity, convex functions, the Lp spaces, the Minkowski and Holder inequalities, convergence and completeness, Bounded linear functionals on Lp spaces..

Books Recommended:

1. H.L. Royden, Real Analysis(4th edition), Macmillan Publishing Company, 1993.

References:

1. G. de. Barra, Measure Theory and Integration, Wiley Eastern Limited, 1981.
2. Lebesgue Measure and integration: an introduction, Frank Burk, Wiley Interscienc Publication, 1998.
3. Inder K. Rana, An Introduction to Measure and Integration, Narosa Publishing House, Delhi, 1997.

E-references:

1. http://www.math.dauniv.ac.in/Dr.MaheshNDumaldar.php
2. Review of Lebesgue Measure and Integration, Christopher E. Heil, School of Mathematics Georgia Institute of Technology
   http://people.math.gatech.edu/~heil/handouts/real.pdf
3. Measure Theory and Lebesgue Integration, Joshua H. Lifton
   http://web.media.mit.edu/~lifton/snippets/measure_theory.pdf
4. The Lebesgue Measure and Integral, Mike Klaas
   http://www.cs.ubc.ca/~klaas/research/lebesgue.pdf

M 213
TOPOLOGY – II

Pre-requisites: M113

Unit I:

Compactness. Continuous functions and compact sets. Basic properties of compactness. Compactness and finite intersection property. Sequentially and Countably compact sets.

Unit II:

Local compactness and one-point compactification. Compactness in metric spaces. Equivalence of compactness, Countable compactness and Sequential compactness in metric spaces. Nets.

Unit III:

First and second countable spaces. Lindelof's theorems. Second countability and separability. Countability and product spaces. Separation axioms. T_0, T_1, T_2, T_3, T_4; their characterizatrion and basic properties. Urysohn's lemma.

Unit IV:

Tietze extension theorem. Urysohn (metrization) embedding theorem. Separation axioms and product spaces. The Tychonoff's theorem. Stone-Cech compactification.
Metrization theorems and paracompactness: Local finiteness. The Nagata-Smirnov metrization theorem. Paracompactness. The Smirnov metrization theorem.

Unit V:

The fundamental group and covering spaces : Homotopy of paths. The fundamental group. Covering spaces. The fundamental group of the circle and the fundamental theorem of algebra.

Books Recommended :

1. James R. Munkres, Topology (Second edition), Prentice-hall of India
2. George F. Simmons, Introduction to topology and modern analysis,McGraw Hill Book Company Inc.

References :

1. N. Bourbaki, General topology, Springer-verlag.
2. K.D.Joshi, Introduction to topology, Wiley Eastern.
3. J.L.Kelley, General topology, Affiliated East-West press Pvt Ltd.

E-references:

1. Topology Course Lecture Notes Aisling McCluskey and Brian McMaster
   http://at.yorku.ca/i/a/a/b/23.htm
2. Notes on Introductory Point-Set Topology, Allen Hatcher
   http://www.math.cornell.edu/~hatcher/Top/TopNotes.pdf
3. Introduction to Topology, Renzo
   http://www.math.colostate.edu/~renzo/teaching/Topology10/Notes.pdf
4. Topology Lecture Notes, Thomas Ward, UEA
   http://www.uea.ac.uk/~h720/teaching/topology/materials/topology.pdf

M 214
COMPLEX ANALYSIS-II

Pre-requisites: Basic Metric space theory: relevant parts of reference [1]

Unit I:
Spaces of analytic functions, Hurwitz's theorem, Montel's theorem,Riemann Mapping theorem, Weierstrass Factorisation theorem.

Unit II: Gamma function & it's properties, Riemann Zeta function, Riemann's functional equation, Runge's theorem and Mittag-Leffler's theorem.

Unit III: Analytic continuation, uniqueness of direct analytic continuation and analytic continuation along a curve, power series method of analytic continuation, Schwartz Reflection Principle, Monodromy theorem and it's consequences.

Unit IV: Harmonic functions on a disk, Dirichlet problem, Green's function.

Unit V: Canonical products, Jensen's formula, order of an entire function, exponent of convergence,Hadamard's factorization theorem, range of an analytic function,Bloch's theorem, The Little Picard theorem, Schottky's theorem, Great Picard theorem.

Books Recommended:

1.J.B.Conway : Functions of one Complex variable, Springer-verlag.
2. S.Ponnusamy : Foundations of Complex Analysis, Narosa Pub, `97

References :

1. Alfohrs : Complex Analysis

E-references:

1. Introduction to Complex Analysis

   http://rutherglen.science.mq.edu.au/wchen/lnicafolder/lnica.html

2. Complex Analysis

   www.umn.edu/~arnold/502.s97/complex.pdf

M 201

DIFFERENTIAL EQUATIONS-II

Pre-requisites: M101

Unit I:
Poincare- Bendixson theory: Autonomous systems, Umlanfsatz, index of a stationary point, Poincare- Bendixson theorem, stability of periodic solutions,

Unit II:
rotation points, foci, nodes and saddle points. Linear second order equations : Preliminaries, Basic facts, Theorems of Sturm,

Unit III:
Sturm-Liouville boundary value problems, Number of zeros,

Unit IV:
Nonoscillatory equations and principal solutions, Nonoscillation theorems.

Unit V:
Use of Implicit function and fixed point theorems : Periodic solutions, linear equations, nonlinear problems.

Books recommended :
1. P.Hartman, Ordinary differential equations, John Wiley, 1964.

References :

1. W.T.Reid, Ordinary differential equations, John Wiley & sons, New York,1971.
2. E.A.Coddigton & N.Levinson, Theory of ordinary differential equations, McGraw Hill, NY, 1955.

E-references:

1. Ordinary Differential Equations, Modern Perspective Mohan C Joshi IITBombay
   http://www.math.iitb.ac.in/~mcj/root.pdf
2. Differential Equations, Paul Dawkins
   http://tutorial.math.lamar.edu/pdf/DE/DE_Complete.pdf
3. Ordinary Differential Equations-Lecture Notes, Eugen J. Ionascu
   http://math.columbusstate.edu/ejionascu/papers/diffeqbook.pdf

SEMESTER – III

M 311

INTEGRATION THEORY

Pre-requisites: Lebesgue Measure theory [1]

Unit I:

Measure spaces, Measurable functions, Integration, Convergence theorems.

Unit II: Signed measures, The Radon-Nikodym theorem, Lebesgue decomposition, L^P spaces, Riesz representation theorem.

[1] Chapter 11

Unit III: Outer measure and measurability, The extension theorem, Lebesgue- Steiltjes integral, Product measures, Fubini's theorem.

[1] Chapter 12, Sections 1,2,3,4.

Unit IV: Baire sets, Baire Measure, Continuous functions with compact support, Regularity of measures on locally compact spaces.

Unit V: Integration of continuous functions with compact support, Riesz- Markoff theorem.

[1] Chapter 13.

Recommanded Books :

1. H.L. Royden, Real Analysis, Mc millan Pub. Co. Inc. New York, 4th Edition, 1993.
2. G.de.Barra., Measure Theory and Integration, Wiley Eastern Limited, 1981
3. Inder K. Rana. An introduction to Measure & Integration Narosa Pub. House, Delhi,1997.
4. P.K. Jain, N.P. Gupta, Lebesgure Measure and Interation New Age International (P) Ltd., New Delhi, 1986.

E-references:

1. Notes on measure and integration in locally compact – Mathematics

   http:/math.berkeley.edu/~arveson/Dvi/rieszMarkov.pdf

M 312

FUNCTIONAL ANALYSIS

Pre-requisites: Metric spaces, compactness, connectedness.

Unit I:
Completion of a metric space, Normed linear spaces. Banach spaces and examples. Quotient space of normed linear space and its completeness.

Unit II:
Equivalent norms. Riesz lemma, basic properties of finite dimensional normed linear space and compactness. Weak convergence and bounded.

Unit III:
linear transformations, normed linear spaces of bounded linear transformations, dual spaces with examples. Open mapping and closed graph theorems. Uniform boundedness theorem and some of its consequences, the Hahn-Banach theorem.

Unit IV:
Reflexive spaces. Weak sequential compactness.

Unit V:
Inner product spaces. Hilbert spaces. Orthonormal sets. Bessel's inequality. Complete orthonormal sets and Parseval's identity. Structure of Hilbert spaces. Projection theorem, Riesz representation theorem. Adjoint of an operator on a Hilbert space. Reflexivity of Hilbert spaces. Self-adjoint operators, positive, projection, normal and unitary operators.

Recommended Books :

1. H.L. Royden, Real Analysis, Macmillan Publishing Co. Inc. New York, 4th Edition, 1993.
2. G.F. Simmons, Introduction to Topology and Modern Analysis, McGraw- Hill Book Company, New York, 1963.
3. E. Kreyszig, Introductory Functional Analysis with Applications, John Wiley & Sons. New York, 1978
4. B.V. Limaye, Functional Analysis, New Age Intergration (P) Ltd., 1996

E-references:

1. An introduction to some aspects of functional analysis, Stephen Semmes, Rice University http://math.rice.edu/~semmes/fun2.pdf
2. http://www.math.dauniv.ac.in/Dr.MaheshNDumaldar.php

M 313

PARTIAL DIFFERENTIAL EQUATIONS

Unit I:

Examples of PDE. Classification. Transport Equation-Initial Value Problem. Non-homogeneous Equation.

Unit II:

Laplace's Equation - Fundamental Solution, Mean Value Formulas, Properties of Harmonic Functions, Green's Function,Energy Methods. Heat Equation- Fundamental Solution, Mean Value Formula, Properties of Solutions, Energy Methods.

Unit III:

Wave Equation-Solution by Spherical Means, Non- homogeneous Equations, Energy Methods.

[1] Chapter 1 Art. 1.1, 1.2, Chapter. 2

Unit IV:

Nonlinear First Order PDE-Complete Integrals, Envelopes, Characteristics,

Unit V:

Hamilton-Jacobi Equations (Calculus of Variations, Hamilton's ODE, Legendre Transform, Hopf-Lax Formula, Weak Solutions, Uniqueness),

[1] Chapter. 3 Art. 3.1 to 3.3

Recommended Books:

1. L.C. Evans, Partial Differential Equations, Graduate Studies in Mathematics, Volume 19, AMS, 1998.

Reference Books:

1. I. N. Sneddon, Elements of Partial Differential Equations, Mc Graw-Hill Book Company, 1985.
2. F. John, Partial Differential Equations, Third Edition, Narosa Publishing House, New Delhi, 1979.
3. P. Prasad and R. Ravidran, Partial Differential Equations, New Age International (P) Limited, Publishers, 1985.

E-references:

1. PARTIAL DIFFERENTIAL EQUATIONS MA 3132 LECTURE NOTES, B. Neta (http://www.math.nps.navy.mil/~bneta/pde.pdf)
2. Notes for Partial Differential Equations, Kuttler (http://www.math.byu.edu/~klkuttle/547notesB.pdf)

M 301

THEORY OF LINEAR OPERATORS-I

Pre-requisites: Basic linear algebra and basic functional analysis.

Unit I:

Spectral theory of normed linear spaces, resolvent set and spectrum, spectral properties of bounded linear operators, properties of resolvent and spectrum.

[1] Chapter 7

Unit II:

spectral mapping theorem for polynomials, spectral radius of bounded linear operator on a complex Banach space, elementary theory of Banach Algebras. [1] Chapter 7

Unit III:

Basic properties of compact linear operators. [1] Chapter 8

Unit IV:

Behaviour of Compact linear operators with respect to solvability of operator equations, Fredholm type theorems, Fredholm alternative theorem, Fredholm alternative for integral equations. [1] Chapter 8

Unit V:

Spectral properties of bounded self-adjoint linear operators on a complex Hilbert space, positive operators, Monotone sequence theorem for bounded self-adjoint operators on a complex Hilbert space, square roots of a positive operator, projection operators.

[1] Chapter 9, Sec 9.1-9.6

Recommended Book:

1. E.Kreyszig, Introductory Functional Analysis with applications, John-Wiley & Sons, New York, 1978.

Reference Books:

2. N.Dunford & J.T.Schwartz,Linear operators-3 parts, Interscience Wiley, New York, 1958-71.
3. P.R. Halmos, Introduction to Hilbert spaces and the theory of spectral multiplicity, second edition, Chelsea Pub. Co., N.Y. 1957.
4. P. R. Halmos, A Hilbert space problem book, D. Von Nostrand company Inc., 1967.

M 302

Linear Programming - I

Pre-requisites: Finite dimensional vector spaces, Linear transformations, Linear system of equations, basic solutions

Unit I:

Inverse of matrix by partition, product form of the inverse, basis to basis lemma, lines & hyperplanes, Convex sets and hyperplanes, polyhedral sets, extreme points, faces, directions and extreme directions, Decomposition theorem for polyhedra, Farkas' lemma.

Unit II:

Theory of simplex method, reduction of any feasible solution to a basic feasible solution, improving a basic feasible solution, unbounded solutions, optimality conditions, alternate optima, extreme points and basic feasible solutions,

Unit III:

computational aspects of the simplex method, initial basic feasible solution, inconsistency and redundancy, review of the simplex method, Big M method, two phase method

Unit IV:

resolution of degeneracy, Charne's perturbation method, Blande's rule, Revised simplex method, the simplex method for bounded variables.

Unit V:

Network Analysis: Shortest path problem, minimum spanning tree problem, Maximum flow problem, Minimum cost flow problem, Network simplex method.

Recommended Books:

1. G. Hadley, Linear programming, Narosa Publishing House, 1995.
2. Mokhtar S. Bazaraa, John J. Jarvis, Hanis D. Sherali, Linear Programming And Network Flows, 2nd Ed, Wiley-India, 2008
3. Schrijver, A.: Theory of Linear and Integer Programming, J. Wiley, 1986

Reference Books:

1. Dantzig G., Thapa M. Linear programming. Vol.1.. Introduction, Springer,1997
2. G.B. Dantzig, M. Thapa: Linear Programming 2: Theory and Extensions, Springer Verlag, 2003
3. G.Hadley, Linear Algebra, Addison – Wesley Pub. Co. Read. Mass. 1961
4. Nemhauser G.L., Wolsey L.A., Integer and combinatorial optimization, Wiley, NewYork, 1988
5. Chvatal V., Linear programming, Freeman, NewYork, 1983
6. Vanderbei R.J., Linear programming: Foundations and extensions, Kluwer Academic Publishers, Boston, MA, 1996

E-references:

1. http://www.math.dauniv.ac.in/Dr.MaheshNDumaldar.php
2. Activity Analysis of Production and Allocation, Proceedings of a Conference, TJALLING C. KOOPMANS
3. National Programme on Technology Enhanced Learning.(Mathematics)

SEMESTER – IV

M 411
MECHANICS

Unit I:

Generalized coordinates. Holonomic and Non-holonomic Systems. Scleronomic and Rheonomic Systems. Generalized potential.

Unit II:

Lagrange's equations of first kind. Lagrange's equations of second kind. Uniqueness of solution. Energy equation for conservative fields. Hamilton's variables. Donkin's theorem. Hamilton canonial equations. Cyclic coordinates. Routh's equations.

Unit III:

Motivating problems of calculus of variations, Shortest distance. Minimum surface of revolution. Brachistochrone problem. Isoperimetric problem. Geodesic. Fundamental lemma of calculus of variations. Euler's equation for one dependent function and its generalization to (i) `n' dependent functions (ii) higher order derivatives. Conditional extremum under geometric constraints and under integral constraints.

Unit IV:

Hamilton's principle, Principle of least action.

[2] Art. 1-6 & relevant parts of 8, 11-14, 16,20, [3] Relevant portion for Calculus of variations.

Unit V:

Poincare Cartan integral invariant. Whittaker's equations. Jacobi's equations. Statement of Lee Hwa Chung's theorem. Hamilton-Jacobi equation. Jacobi theorem. Method of seperation of variables. Lagrange brackets. Poisson's bracket. Poisson's identity. Jacobi-Poisson Theorem. Condition of canonical character of a transformation in terms of Lagrange brackets and Poisson brackets. Invarience of Lagrange brackets and Poisson brackets under canonial transformations.

[2] Art. 15, 18, 20, 22, 24-27, 30, 32.

Books Recommended :

1. F. Gantmacher, Lectures in Analytic Mechanics, MIR Publishers, Moscow, 1975.

Reference Books:

1. H. Goldstein, Classical Mechanics (2nd Edition), Narosa Publishing House, New Delhi.
2. Narayan Chandra Rana and Pramod Sharad Chandra Joag, Classical Mechanics, Tata McGraw Hill, 1991.
3. Louis N. Hand and Janet D. Finch, Analytical Mechanics, Cambridge University Press, 1998.

M 401

THEORY OF LINEAR OPERATORS – II

Pre-requisites: M 301

Unit I:

Spectral family of a bounded self-adjoint linear operator and it's properties, spectral representation of bounded self-adjoint linear operators, spectral theorem
[1] Chapter 9, Sec 9.7-9.11

Unit II:

Unbounded linear operators in Hilbert space, Hellinger-Toepliz theorem. [1] Chapter 10

Unit III:

Hilbert adjoint operators, Symmetric and self-adjoint linear operators, closed linear operators and closures, spectrum of an unbounded self-adjoint linear operator.
[1] Chapter 10

Unit IV:

spectral theorem for unitary and self adjoint linear operators. [1] Chapter 10

Unit V:

Multiplication operator and Differentiation operator. [1] Chapter 10

Recommended Book:

1 E.Kreyszig, Introductory Functional Analysis with applications, John-Wiley & Sons, New York, 1978.

Reference Book:

2 N.Dunford & J.T.Schwartz,Linear operators-3 parts, Interscience Wiley, New York, 1958-71.

M 402

Linear Programming –II

Pre-requisites: M401

Unit I:

Duality theory, weak and strong duality theorems, Complementary slackness, dual simplex method, primal dual algorithm, Integer programming, the KKT conditions.

Unit II:

Transportation problems, properties of the activity matrix of a transportation problem, simplification of the simplex method to the transportation problem, bases in a transportation problem, the stepping stone algorithm, resolution of degeneracy, determination of an initial basic feasible solution, alternative procedure for computing z_{ij} $-c_{ij}$ using duality(u-v method).

Unit III:

Assignment problems, reduced cost coefficient matrix, the Hungarian method, Konig – Evergary theorem, The Birkoff –von Neumann theorem.

Unit IV:

Sensitivity analysis, the Dantzig-Wolf decomposition, Game theory and linear programming, Two person zero sum games, Games with mixed strategies, Graphical solution, Solution by linear programming.

Unit V:

Applications: Optimal product mix and activity levels, Petroleum refinery operations, Blending problems, Economic interpretation of dual linear programming problems, Input output analysis, Leotief systems.

Recommended Books:

1. G. Hadley, Linear programming, Narosa Publishing House, 1995.
2. Mokhtar S. Bazaraa, John J. Jarvis, Hanis D. Sherali, Linear Programming And Network Flows, 2Nd Ed, Wiley-India, 2008
3. Schrijver, A.: Theory of Linear and Integer Programming, J. Wiley, 1986

Reference Books:

1. Dantzig G., Thapa M. Linear programming. Vol.1.. Introduction, Springer,1997
2. G.B. Dantzig, M. Thapa: Linear Programming 2: Theory and Extensions, Springer Verlag, 2003
3. G.Hadley, Linear Algebra, Addison – Wesley Pub. Co. Read. Mass. 1961
4. Nemhauser G.L., Wolsey L.A., Integer and combinatorial optimization, Wiley, NewYork, 1988
5. Chvatal V., Linear programming, Freeman, NewYork, 1983
6. Vanderbei R.J., Linear programming: Foundations and extensions, Kluwer Academic Publishers, Boston, MA, 1996

E-references:

1. http://www.math.dauniv.ac.in/Dr.MaheshNDumaldar.php
2. Activity Analysis of Production and Allocation, Proceedings of a Conference, TJALLING C. KOOPMANS
3. National Programme on Technology Enhanced Learning.(Mathematics)

M 403

HOMOTOPY THEORY

Pre-requisites: M113 & M213

Unit I:

The Fundamental Group, Homotopic Paths and the Fundamental Group.

Unit II:

The Covering Homotopy Property for S^{1}, Examples of Fundamental Groups.

[1] Chapter 4.

Unit III:

Covering Spaces, The Definition and Some Examples, Basic Properties of Covering Spaces, Classification of Covering Spaces, Universal Covering Spaces, Applications. [1] Chapter 5.

Unit IV:

The Higher Homotopy Groups, Equivalent Definitions of $\pi_n(X, x_0)$, Basic Properties and Examples.

Unit V:

Homotopy Equivalence, Homotopy Groups of Spheres.[1] Chapter 6.

Recommended Book:

1. F. H. Croom : Basic Concepts of Algebraic Topology, Springer-Verlag New York.
2. W.S. Massey : Algebraic Topology, Springer -Verlag.
3. E.H. Spanier : Algebraic Topology : Mc Graw – Hill Book Company.

M 404

TOPICS IN RING THEORY

Pre-requisites: Basic definitions and results concerning rings and fields.

Unit I:

Rings and Ring Homomorphisms, Ideals Quotient Rings, Zero Divisors, Nilpotent Elements, Units.

Unit II:

Prime Ideals and Maximal Ideals, Niltradial & Jacobson Radial Operations an Ideals, Extension & Contraction.

Unit III:

Modules,Operation on Submodules, Direct Sum and Product of Modules, Restriction and Extension of Scalars.

Unit_IV:

Tensor product of modules, basic properties ,Exactness Properties of Tensor Product, Algebras & Tensor Product of Algebras.

Unit-V:

Rings and Modules of Fractions, Local Properties Extended and Contracted Ideals in Ring of Fractions. (with Emphasis an Exercise) [1 chapter 1 to 3]

Books Recommended :

1. Introduction to Commutative Algebra, Atiyah & I.G. Macdonald,
   Addison – Wesley Pub. Co

E-references:

1. **Commutative Algebra Notes** Branden Stone
   math.bard.edu/~bstone/commalg-**notes**/
2. **Commutative Algebra** Lecture **Notes** - Tata Institute of Fundamental
   www.math.tifr.res.in/~anands/CA-Lecture%20**notes**.pdf

M 405

ALGEBRAIC TOPOLOGY

Pre-requisites: M113 & M213

UNIT I :

Deformation retracts and homotopy type. Fundamental group of S for $n > 1$, and some surfaces. The Jordan seperation theorem, the Jordan curve theorem, Imbedding graphs in plane.

[1] Chapter 9, sections 58 to 60 & Chapter 10, sections 61, 63 and 64.

UNIT II :

Free product of groups, Free groups, The Siefert- van Kampen theorem and its applications. Classification of surfaces : Fundamental groups of surfacees, Homology of surfaces, Cutting and pasting, Construction of Compact surfaces, The classification theorrem.

[1] Chapter 11, sections 68 to 73 & Chapter 12, sections 74 to 78.

Unit III :

Equivalence of covering spaces, Covering transformations, The universal covering space, and its existence.: Homology groups of a simplicial complex : Simplicial complexes and simplicial maps, Homology groups, Homology groups of surfaces, Zero-dimensional homology, The homology of a cone, Relative homology, Homomorphisms induced by simplicial maps, Chain complexes and acyclic carriers. [1] Chapter 13. [2] Chapter 1, Sections 1 to 9, 12 & 13.

UNIT IV :

Relative homology : The exact homology sequence, Mayer-vietoris sequences, The Eilenberg-Steenrod axioms (without proofs). The singular homology groups, The axioms for Singular theory (without proofs), Mayer-Vietoris sequences, The isomorphism between simplicial and singular homology, CW complexes, The homology of CW complexes and application to Projective spaces and Lens spaces.

[2] Chapter 3, Sections 23 to 28 (relevant portions)

Chapter 4, Sections 29 to 34 & 37 to 40 (relevant portions)

UNIT V :

Cohomology : The Hom functor, Simplicial cohomology groups, Relative cohomology, The cohomology of frre chain complexes, The cohomology of CW complexes, Cup products, Cohomology ring of surfaces.

[2] Chapter 5, Sections 41 to 49.

Books recommended :

[1] J.R. Munkres, Topology, Second edition, Prentice-Hall of India, 2000.

[2] J.R. Munkres, Elements of Algebraic topolgy, Addison-Wesley Publishing company, 1984.

M 406

Analytic Number Theory

Unit I: Characters of finite abelian groups, The character group, Dirichlet characters, Sums involving Dirichilet characters, Dirichlet's theorem on primes in arithmetic progressions. [1] Chapter 6, sections 6.5 to 6.10, Chapter 7

Unit II: Dirichlet series and Euler products, the function defined by Dirichlet series, The half-plane of convergence of a Dirichlet series, Integral formula for the coefficients of Dirichlet series, etc. [1] Chapter 11

Unit III: Properties of the gamma functions, Integral representations of Hurwitz zeta functions, Analytic continuation of hurwitz zeta functions, Functional equation for the Riemann zeta function and properties of Riemann zeta functions etc. [1] Chapter 12

Unit IV: Analytic proof of prime number theorem. [1] Chapter 13

Unit V: Geometric representation of partitions, Generating functions of partitions, Euler's pentagonal number theorem, Euler's recursion formula for p(n), Jacobi's triple product identity, The partition identity of Ramanujan. [1] Chapter 14

Book Recommneded:

[1] T. M. Apostol, Introduction to Analytic Number Theory, Narosa Pub, House, 1989.

M 407

Abstract Harmonic Analysis

Unit I : Definition of a topological group and its basic properties. Subgroups and quotient groups. Product groups & projective limits. [1], Sections 4,5,6 of Chapter Two.

Unit II : Properties of topological groups involving connectedness. Invariant pseudo-metrics and separation axioms. Structure theory for compact and locally compact Abelian groups. Some special locally compact Abelian groups. [1], Sections 7,8,9,10 of Chapter Two.

Unit III : The Haar integral. Haar Measure. Invariant means defined for all bounded functions. Invariant means of almost periodic functions. [1], Chapter Four.

Unit IV : Convolutions, Convolutions of functions and measures. Elements of representation theory. Unitary representations of locally compact groups. [1], Chapter Five.

Unit V : The character group of a locally compact Abelian group and the duality theorem. [1], Sections 23,24 of Chapter Six.

Recommended Book :

1. Edwin Hewitt and Kenneth A. Ross, Abstract Harmonic Analysis-I, Springer-Verlag, Berlin, 1993.

Reference :

2. Lynn H. Loomis, An introduction to abstract harmonic analysis, D. Van Nostrand Co. Princeton.

M.Sc. Mathematics

IV Semester

M 405: Mathematical Modelling (CBCS)

Unit -I

Queuing Theory and Mathematical Modelling : Introduction of Queue Theory, queuing models Poisson processes, Queuing theory Kendall notation of queuing problems, Transient and Steady State Condition, Mathematical models in Queue system models : M/M/I/Infinite/FCFS, M/M/I/Finite/FCFS, M/M/S/Infinite/FCFS and Numerical Problems

Unit -II

Stochastic Process and Markov Chain with properties, Transition Probability and Probability Vector, Steady State (Or Equilibrium Condition), Regular and Eargodic Markov Chain

Unit -III

Mathematical Modeling Through Graphs : Situation that can be modeled through graph and matrix representation of graph, Mathematical Models in terms of Directed Graph, Mathematical Models in terms of Signed Graph, Mathematical Models in terms of directed graph Weighed Graph.

Unit -IV

Mathematical Modeling through Calculus of Variations, Optimization Principles and techniques of Optimization.

Unit -V

Some Mathematical models in real world problem of Physics, Biological Sciences, Physical Sciences and Social Sciences.

References :

1. Mathematical Modelling : J.N. Kapur, New Age Publications.
2. Mathematical Modelling in Biology and Medicine : J.N. Kapur, New Age Publications.
3. Advanced Computational Mathematics : D.C.Agrawal, Shri Sai Prakashan.
4. Introduction to Mathematical Modelling, Edward A. Bender, Dover Publications Inc.,New York, USA.
5. Operations Research : Kanti Swarup , Sultan Chand & Sons.

M 305

MATHEMATICAL MODELING

Unit I:

Simple situation requiring mathematical modelling. Techniques, classification and characteristics of mathematical models .Limitations of mathematical modelling.

Unit II:

Setting up first order differential equations, qualitative solution, stability of solutions,growth and decay population models , exponential and logistic population models.

Unit III:

Compartment models through system of ODE. Mathematical models in medicine, arms race, battles and international trade in terms of systems of ODE.

Unit IV:

Non-linear difference equations models for population growth probability generating function, fourth method of obtaining partial differential equation models. PDE model for a stochastic epidemic process with no removal. Model for traffic on a highway.

Unit V:

General Communication networks, general weighted digraphs, map-colouring problems.

References:

1. Kapoor JN : Mathematical models in biology and medicine EWP(1985)

2. Martin Brann C.S Coleman , DA Drew(Eds) differential equation models.

3. C.L.Liu , Elements of discrete mathematics.

4. A.M.Law and W.D Ketton , Simulation modeling and analysis , McGraw Hill Intl. Ed(Second edition)1991.

SCHEME OF EXAMINATION

M. Phil. Mathematics

M. Phil. Semester I

CODE	SUBJECT	Credits (L)	Credits (P)	Total Credits
MP 111	Review of Literature	-	-	6
MP 112	Research Methodology	4	4	8
MP 113	Computer Applications	2	2	4
MP 101*	Linear Algebra Over Commutative Rings	4	-	4
MP 102*	Homology Theory	4	-	4
MP 103*	Algebraic Graph Theory	4	-	4
MP 104*	Combinatorial Matrix Theory	4	-	4
MP 105*	Commutative Rings	4	-	4
	Comprehensive Viva-Voce			4
	Total Credits			30

* Students have to opt two out of the five electives.

Contact hours	:	26
Credits	:	30
L	:	Lecture
P	:	Practical

M.Phil. Semester II

CODE	SUBJECT	Credits
MP 211	Seminars	3
MP 212	Term Paper/Assignment	3
MP 213	Dissertation /Project	20
	Comprehensive Viva-Voce	4
	Total Credits	30

SYLLABUS

M111 Review of Literature

Review of a minimum of two research papers (from standard refereed journals) under the guidance of a teacher.

M112 Research Methodology

Part A: Theory: Nonlinear Programming.

Unconstrained Problems, Problems with Inequality Constraints, Problems with Inequality and Equality Constraints, Second-Order Necessary and Sufficient Optimality Conditions for Constrained Problems, The Cone of Tangents, Other Constraint Qualifications, Problems with Inequality and Equality Constraints.

The Lagrangian Dual Problem, Duality Theorems and Saddle Point Optimality Conditions, Properties of the Dual Function, Formulating and Solving the dual Problem, Getting the Primal Solution, Linear and Quadratic Programs.

The Linear Complementary Problem, Quadratic Programming, Separable Programming, Linear Fractional Programming, Geometric Programming.

Definitions and Basic Properties, Subgradients of Convex Functions, Differentiable Convex Functions, Minima and Maxima of Convex Functions, Generalizations of Convex Functions.

Reference Books :

1. Nonlinear Programming, Bazaraa, Sherali, Shetty, John Wiley, 2004.
2. Convex Analysis, Rockafeller R.T., Princeton University press, 1970.
3. Optimization by vector space methods, Luenberger D.G., John Wiley, 1969.
4. Principles of optimization theory, Bector, Chandra, Dutta, Narosa, 2005.
5. Nonlinear Programming, Luenberger, D.G.,

E-references:

- Convex Optimization, Stephen Boyd, Lieven Vandenberghe, Cambridge University Press. http://www.stanford.edu/~boyd/cvxbook/bv_cvxbook.pdf
- Convex Analysis and Optimization, Massachusetts Institute of Technology, Cambridge, Dimitri P. Bertsekas http://web.mit.edu/dimitrib/www/Convex_Slides_2010.pdf

Part B: Practicals/Techniques & Tools

1. Latex and Beamer.
2. Introduction to Mathematical softwares such as Matlab/ Scilab.
3. Working knowledge of INFLIBNET.

M113 Computer Applications

Computer Fundamentals:

Characteristics of Computers, Block Diagram of computer, Generation of Computers Classification of Computers, Memory and Types of Memory, Hardware & Software, System Software, Application Software.

Compiler, Interpreter, Programming Languages, Types of Programming Languages (Machine Languages, Assembly Languages, High Level Languages). Algorithm and Flowchart.

Number system and Information codes: Binary, Octal & Hexadecimal number systems. Conversion from one system to another. Computer Arithmetic: Various operations –addition, subtraction.

Introduction to "C" Language :

C programming: Data types; Operators; Expressions; Scope resolution and variable types; Basic structure of 'C' Program; Control flow structures; Looping: what is looping, while statement, do-while statement, for statement. Arrays, Single dimensional, Multi dimensional array, Functions, Category of functions, Recursion, Mathematical functions, Pointers.

Reference Books :

1. Computer Fundamentals- B.Ram.
2. Computer Fundamentals- P.K. Sinha.
3. Programming in 'C'- E. Balagurusamy.
4. Programming in 'C'- Gottfried.
5. The 'C' Programming Language- B.W. Kernigham & D. M. Ritchie.
6. A Guide to MATLAB: For Beginners And Experienced Users Brian R. Hunt, Ronald L. Lipsman, Jonathan Rosenberg Cambridge University Press, 2006.

List of Programmes :

1. Program for Factorial,
2. Program for sine series, cosine series,
3. Program for $^{n}C_{r}$,
4. Program for Pascal Triangle,
5. Program for Prime number,
6. Program for Factors of a number,
7. Program for Perfect number and GCD of numbers
8. Program for Swapping.
9. Program for Addition and Multiplication of Matrices.
10. Program to find Smallest Element in Array in C Programming
11. Program to find Largest Element in Array in C Programming
12. Program to reversing an Array Elements in C Programming
13. Program to Searching element in array by Linear Search and Binary Search
14. Program to Print Square of Each Element of 2D Array Matrix
15. Program to find Transpose of Given Square Matrix
16. Program to evaluate Subtraction of two matrices (matrix) in C
17. program for addition of two matrices in C
18. Program to Multiply Two 3 X 3 Matrices
19. Program to Convert Binary to Decimal number system
20. Program to Convert Decimal to Binary system
21. Program Even Number Pyramid in C
22. C Program to sort array of Structure in C Programming
23. C Program to Implement Bubble Sort in C Programming
24. C Program to solve L.P.P. using Simplex Method
25. Finding roots of a function by various numerical analytical techniques.

M101 Linear Algebra over Commutative Rings

Basic concepts on modules over commutative rings, direct sums, exact sequences, free modules, projective modules, free modules over a PID, finitely generated modules over PID's, complemented submodules (Chapter 3 & relevant part of Chapter 7), Tensor product of modules.

Matrix algebra, determinants and linear equations, matrix representations of homomorphisms (Section 1 to 3 of Chapter 4).

Canonical form theory, computational examples, matrices over PID's, equivalence and similarity, Hermite and Smith normal forms, computational examples a rank criterion for similarity (Section 4-5 of Chapter 4, Chapter 5).

Recommended Book :

1. Algebra, (An Approach Via Module Theory). William A. Adkins & Stever H. Weintraub. Springer Verlag.

Reference Books :

1. Algebra, S. Lang. Addison -Wesley
2. Commutative Algebra, M.F. Atiyah & I.G. Macdonald.
3. Abstract Algebra, Dummit & Foote., 2nd ed John Wiley & Sons.

M102 Homology Theory

Simplicial complexes, Barycentric Subdivision, Simplicial approximation, the oriented chain complex of a simplicial complex, Simplicial homology groups with integer coefficients, Mayer- Vietoris Sequences, The homology long exact sequence of a pair, Calculations and applications, Singular homology.

Reference Books :

1. A. Dold : Lectures on Algebraic Topology, Springer-Verlag.
2. E.H. Spanier :Algebraic Topology, Mc Graw-Hill.
3. Satya Deo : Algebraic Topology, Hindustan Book Agency.

MP103Algebraic Graph Theory

Prerequisites: Linear Algebra, Elements of Graph Theory

Basic matrix theory, Adjacency matrix, Incidence matrix, Perron-Frobenius Theorm,

Interlacing, strongly regular graphs, the Laplacian of a graph

Cuts and Flows

The rank Polynomial

Reference Books :

1. C. Godsil and G. Royle: Algebraic Graph Theory, Springer
2. R.B.Bapat: Graphs and Matrices, TRIM Series, Hindustan Book Agency.
3. N.L.Biggs: Algebraic Graph Theory, Cambridge University Press.

E-references:

- Reinhard Diestel, Graph Theory
  http://www.esi2.us.es/~mbilbao/pdffiles/DiestelGT.pdf

MP104 Combinatorial Matrix Theory

Prerequisites: Basic Linear algebra

Basic Existence Theorems for Matrices with Prescribed Properties : The Gale–Ryser and Ford–Fulkerson Theorems, Tournament Matrices and Landau's Theorem, Symmetric Matrices

The Class $A(R, S)$ of (0,1)-Matrices**:** A Special Matrix in $A(R, S)$, Interchanges **,** The Structure Matrix $T(R, S)$

The Class $T(R)$ of Tournament Matrices : Algorithm for a Matrix in $T(R)$, Basic Properties of Tournament Matrices, Landau's Inequalities, A Special Matrix in $T(R)$

Transportation Polytopes, Doubly Stochastic Matrices, Basic Properties
Faces of the Assignment Polytope

Reference Books :

1. Combinatorial Matrix Classes, Richard A. Brualdi, Cambridge University Press.
2. Combinatorial Matrix Theory Richard A. Brualdi, Herbert J. Ryser

MP 105 Commutative Rings

Primary Ideals, Primary Decomposition, Isolated & Embedded Primes, Primary Decomposition In Noetharian Rings, Primary Submodules, Associated Primes Of A Module, Noetherian Module, Support of A Module, Dedekind Rings, Krull's Intersection Theorem, Regular Sequences, Quasi-Regular Sequences, Depth, Associated Graded Ring, Generalized Principal Ideal Theorem, Patching Modules, Regular Local Ring, Cohen-Macauley Rings with Emphasis on exercises based on the main concepts.

Reference Books :

1. Commutative Algebra, I.Kapalansky.
2. Commutative Algebra, Matsumura.
3. Introduction to Commutative Algebra, Atiyah & I.G. Macdonald

SCHOOL OF MATHEMATICS

PH114 Advance Course in Mathematics

Unit I:

Functions of Several Variables, derivatives in an open subset of R^n, chain rule, partial derivatives, the contraction principle, inverse function theorem, implicit function theorem.

Unit II:

Definitions and Basic Properties, Subgradients of Convex Functions, Differentiable Convex Functions, Minima and Maxima of Convex Functions, Generalizations of Convex Functions.

Unit III:

Theoretical and computational aspects of Canonical forms, Hermite form, Smith normal form.

Unit IV:

Methods in Commutative Algebra: Localization, Completion, Primary decomposition, Dimension theorem.

Unit V:

Characters of finite abelian groups, The character group, Dirichlet characters, Sums involving Dirichilet characters, Dirichlet's theorem on primes in arithmetic progressions.

Recommended Books:

1. Introduction to Commutative Algebra, Atiyah & Mc Donald.
2. An approach via module theory, Adkis & Weintraub.
3. Principals of Mathematical Analysis, Walter Rudin.
4. Nonlinear Programming, Bazaraa M.S., Sherali H.D., Shetty C.M.
5. Introduction to Analytic Number Theory, T. M. Apostol.